

Integrity 2022
Third Workshop in
Integrity in Social Networks and Media
February 25, 2022

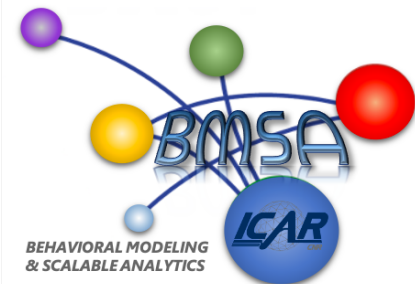


Characterizing Information diffusion

Social Influence, Propagation Speed, Polarization

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Disclaimer & Acknowledgements

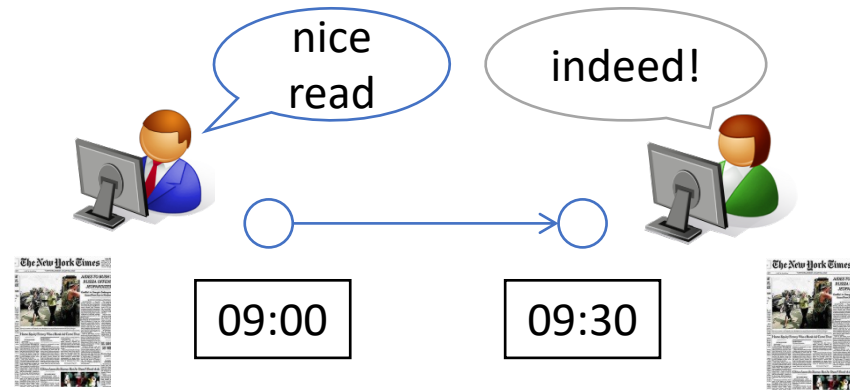
- Summary of results of joint works with Francesco Bonchi, Nicola Barbieri, Corrado Monti, Ettore Ritacco

Agenda

- The Information Diffusion flow
- Influence and susceptibility
- Speed of propagation
- Polarity and echo chambers

Context

Information propagation in on-line social networks



users perform **actions**

post messages, pictures, video

buy, comment, link, rate, share, like, retweet

users are **connected** with other **users**

interact, influence each other

actions propagate

Relevant Questions

- What makes a content popular?
- Which creators are able to trigger a cascade?
- Who will share a content?
- When will someone share a content?
- Who is expert in a topic characterizing a set of contents?
- Who is interested in a topic?
- Which are the most popular topics?
- ...



Basic Notation

- A graph $G = (V, E)$
 - Users u, v in V
- Items i
 - A cascade all (time-sorted) users who adopt that item

Node	Action	Time
u_1	i_1	t_0
u_2	i_1	t_1
u_3	i_2	t_3
...

- $Y_{i,u}$ binary indicator
u adopts i

A Basic Tool: Probabilistic modeling

- Treat data as observations that arise from a generative probabilistic process that includes hidden variables
 - For cascade data, the hidden variables reflect the behavior of single users or the commonality in actions
- Infer the hidden structure using posterior inference
 - What are the latent behaviors that describe this group of users?
- Situate new data into the estimated model.
 - How does a new user fit into the estimated behavioral structure?

Key Insight 1

Propagations are topic-dependent



Key insight 1:

Propagations are topic-aware

Generalization of the IC Model: the probability of a user become active depends on the strength exerted by one of its predecessors, which in turn depends on the **topic k of interest**.

$$\mathcal{L}(i, u) = y_{i,y} \cdot \log \left(\sum_k P_{u,k}^{i,+} \right) + (1 - y_{i,u}) \cdot \sum_k \log P_{u,k}^{i,-}$$

Probability that some of the potential influencers in activating u

$$P_{u,k}^{i,+} = 1 - \prod_v (1 - p_{u,v}^k)$$

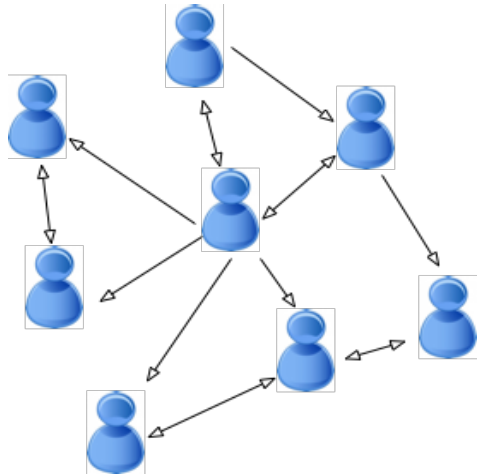
Probability that none of the the “out-of-react” influencers succeeds in activating u

$$P_{u,k}^{i,-} = \prod_v (1 - p_{u,v}^k)$$

Topic-aware Social Influence Propagation Models

Input:

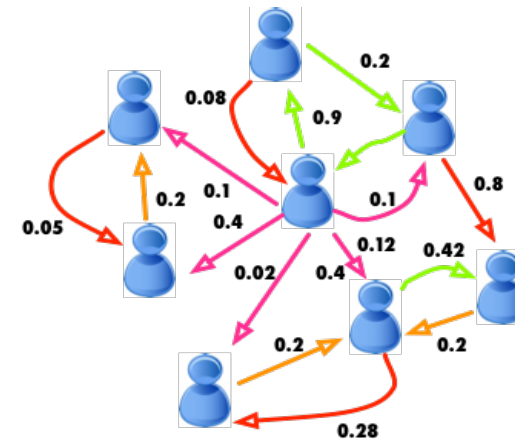
Social Network + Propagation Log
+ number of topics K



Output:

Topics +
Topic-Aware propagation
Strengths

Node	Action	Time
u_1	i_1	t_0
u_2	i_1	t_1
u_3	i_2	t_3
...



Better users' behavior modeling

Applications:

Detection of influent authorities for different topics

Design of targeted viral marketing strategies

Key insight 2

Adoptions and connections depend on influence

Probability of a link

$$P((u, v) \in E) = \vartheta_{u,k} \cdot \varphi_{v,k}$$

(source)

(destination)

$$\vartheta_u = \text{SoftMax}(\Pi^s)$$

$$\varphi_v = \text{SoftMax}(\Pi^d)$$

Probability of an action being propagated

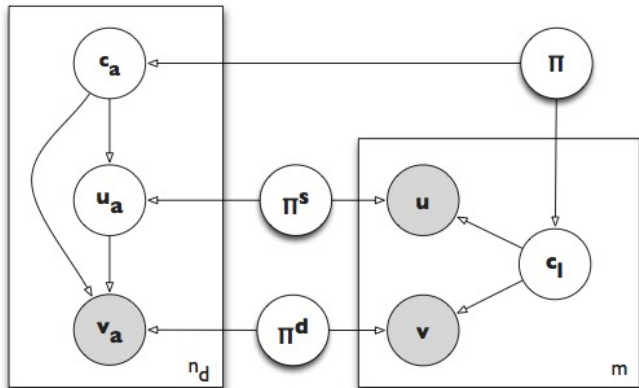
$$p_{u,v}^k \propto \theta_{u,k} \cdot \phi_{k,v}$$

(influencer)

(susceptible)

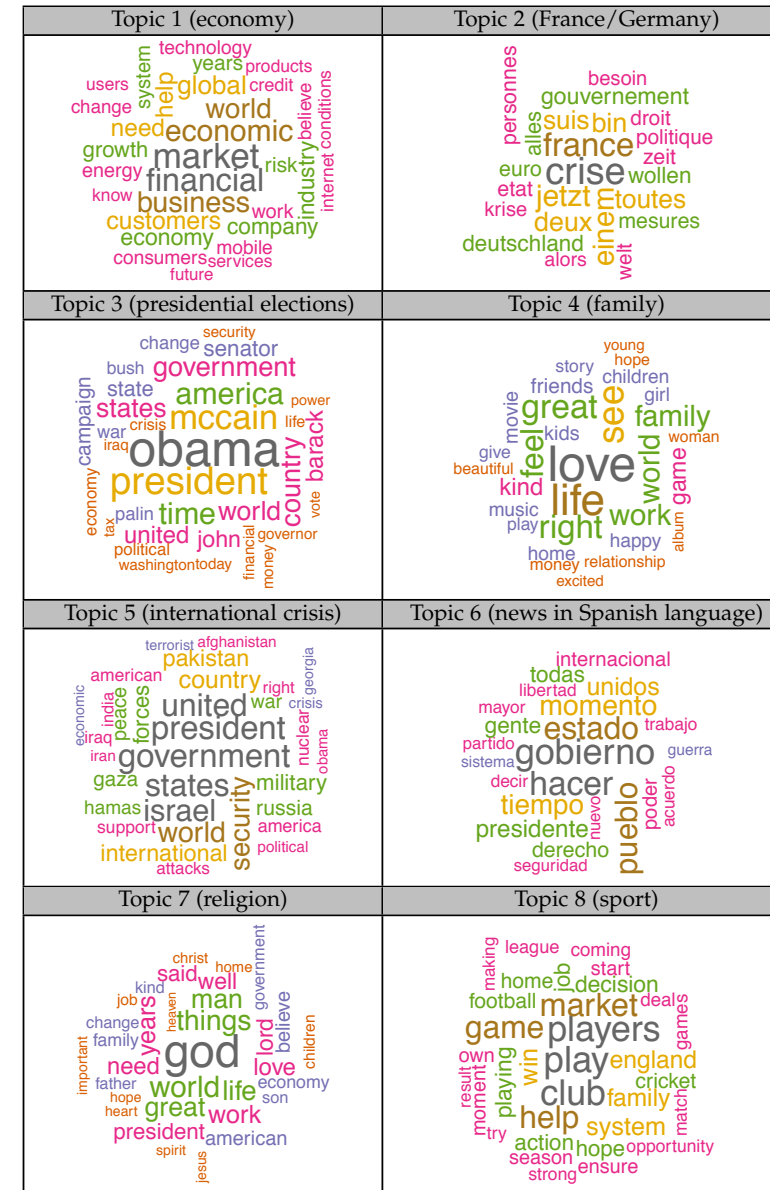
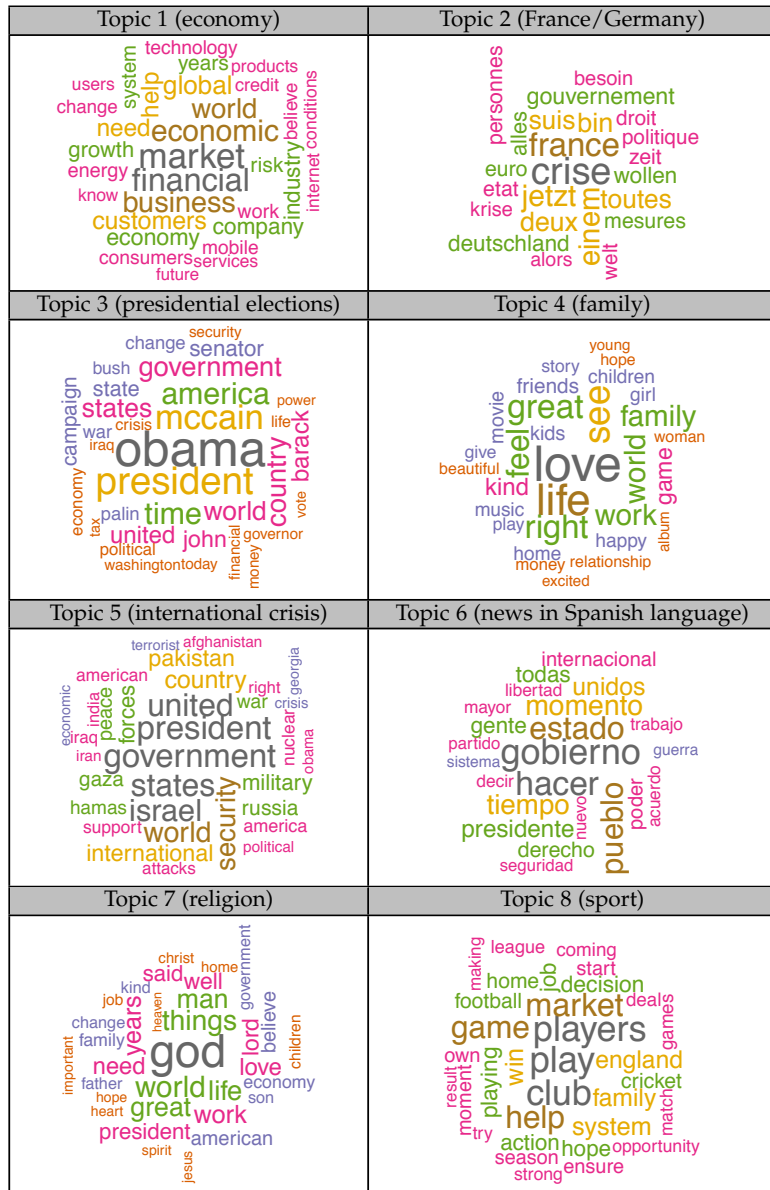
$$\varphi_v = \text{SoftMax}(\Pi^s)$$

$$\theta_u = \text{SoftMax}(\Pi^d)$$



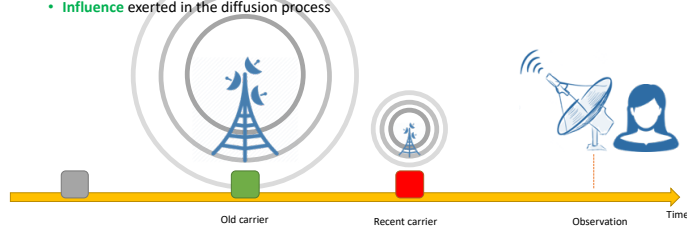
Topics on Memetracker

Influential nodes on Memetracker



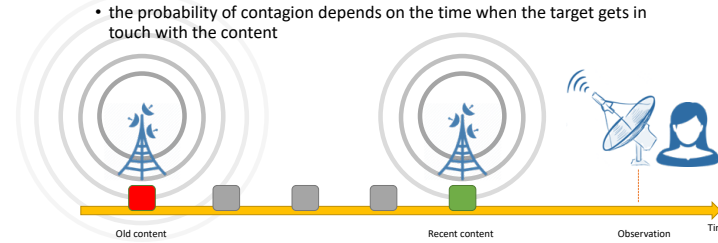
• **Contagion is carrier-dependent**

- Some carriers are more infectious than others
- **Influence** exerted in the diffusion process



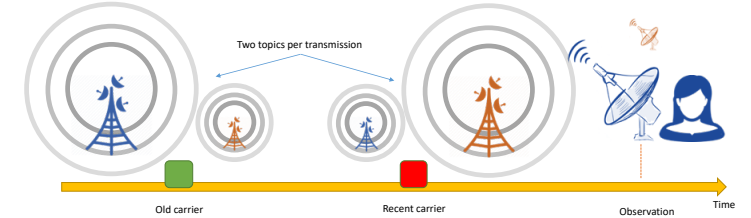
• **Contagion is time-dependent**

- the probability of contagion depends on the time when the target gets in touch with the content



• **Contagion is topic-dependent**

- **Susceptibility** and **influence** are relative the content
- Content is characterized by **topics**



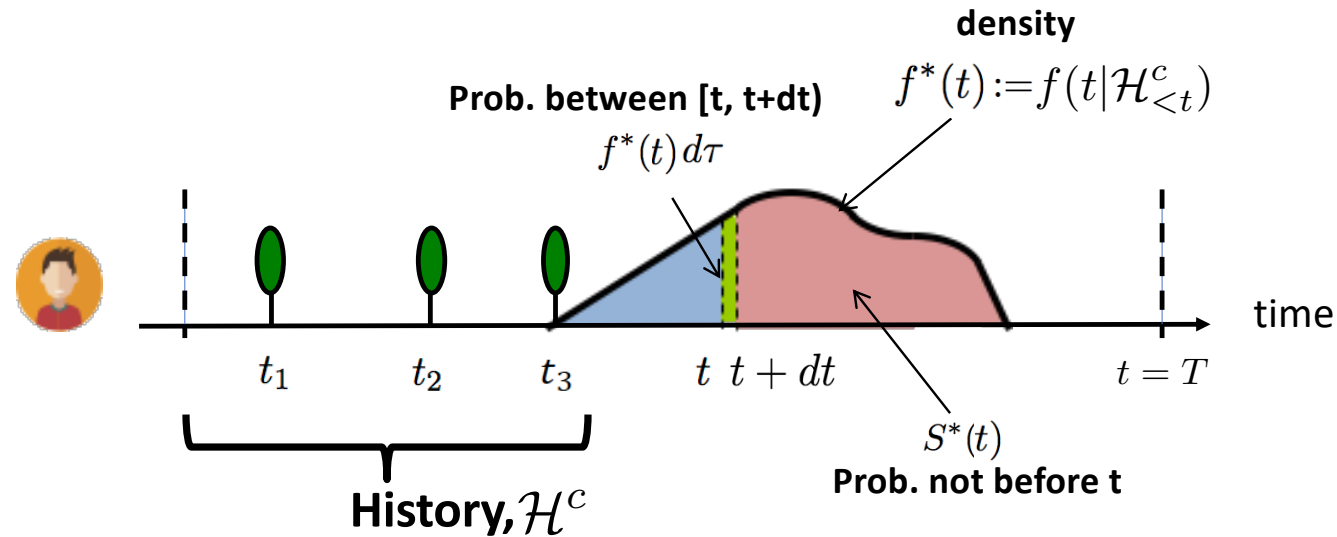
Modeling the contagion process

Key insight 3

The speed of propagations depend on influence

Modeling time as a random variable

Survival Networks



Intensity:

Probability between $[t, t+dt)$ but not before t

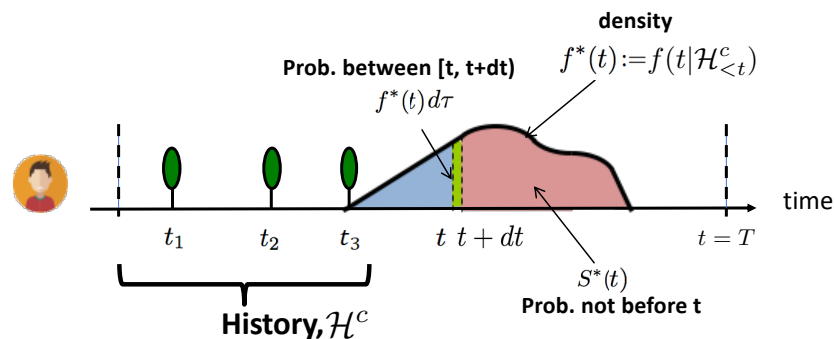
$$\lambda^*(t)dt = \frac{f^*(t)dt}{S^*(t)} \geq 0$$

$\lambda^*(t)$ It is a rate = # of events / unit of time

Modeling time as a random variable

Survival Networks

Idea: model the intensity function as the effect of influence and susceptibility



Intensity:

Probability between $[t, t+dt)$ but not before t

$$\lambda^*(t)dt = \frac{f^*(t)dt}{S^*(t)} \geq 0$$

$\lambda^*(t)$ It is a rate = # of events / unit of time

$$\lambda(t_i | u, v, k) \propto \theta_{u,k} \cdot \phi_{u,k}$$

Node	Action	Time
u_1	i_1	t_0
u_2	i_1	t_1
u_3	i_2	t_3
...

Summary so far

It's all about representation learning!

Authoritativeness of a user in a topic: $\varphi_{u,k}$

Interest of a user for a topic: $\theta_{u,k}$

Relevance of an item for a topic: $\gamma_{i,k}$



Lady Gaga @ladygaga

Justin Bieber @justinbieber



Barack Obama @barackobama

CNN @cnn

The Economist @TheEconomist



0.92



0.08



0.01



0.09

Key insight 4 Polarization and ideological leanings

- We can also use latent representations for modeling polarization
 - **Authoritativeness** of a user in a topic: $\varphi_{u,k}$
 - **Interest** of a user for a topic: $\theta_{u,k}$
 - **Relevance** of an item for a topic: $\gamma_{i,k}$
- **Polarization**

$$\ell_{u,k} \in \{+, -\}$$

- Probability of positive polarization

$$\phi_{u,k} \triangleq P(\ell_{u,k} = +)$$

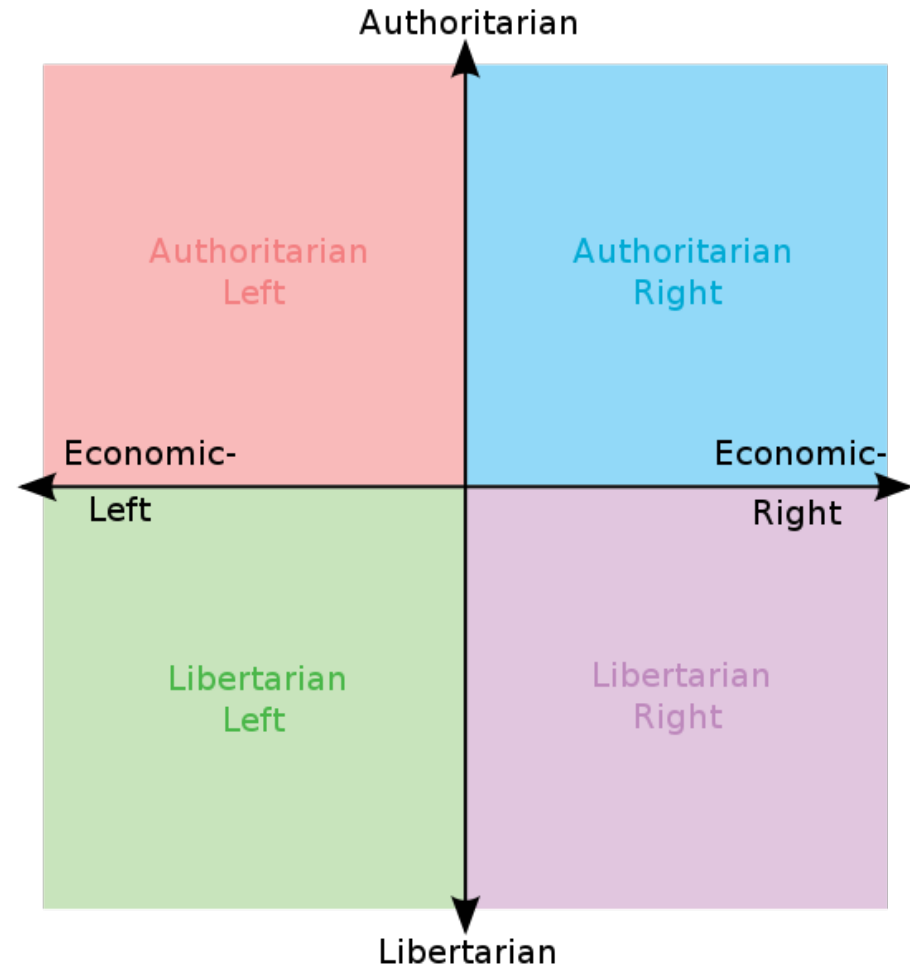
Polarization and ideological leanings

- Many works in opinion modeling assume a single axis
 - Often ill-defined too



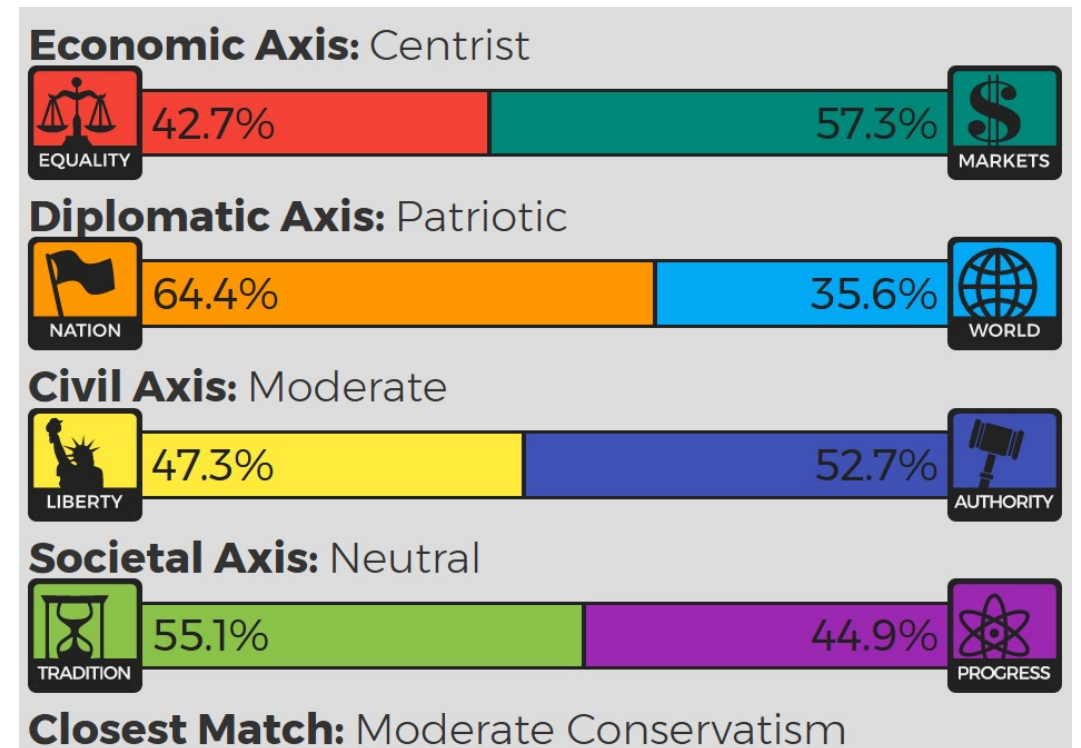
Why ideological embeddings?

- Multi-dimensional ideological spaces



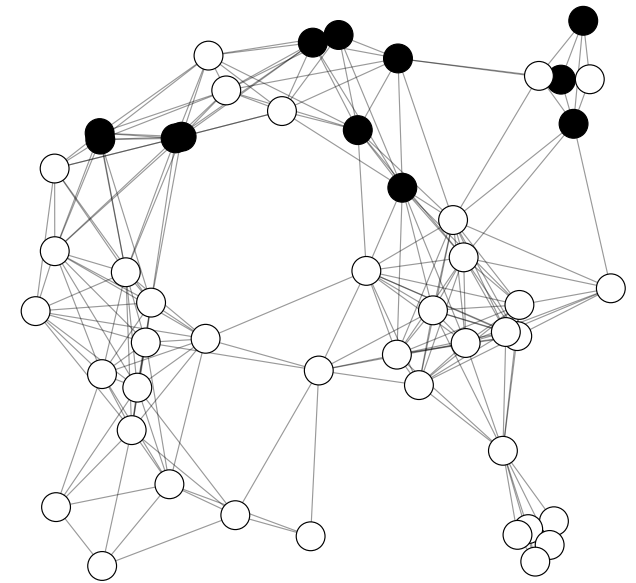
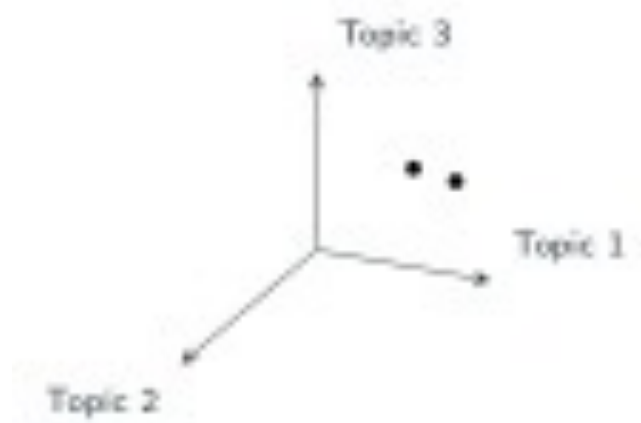
Why ideological embeddings?

- Multi-dimensional ideological spaces



Which behavior makes this observable?

- Spreading news on social media
 - A graph of agents that spread news content
 - They spread the same item if they are ideologically aligned



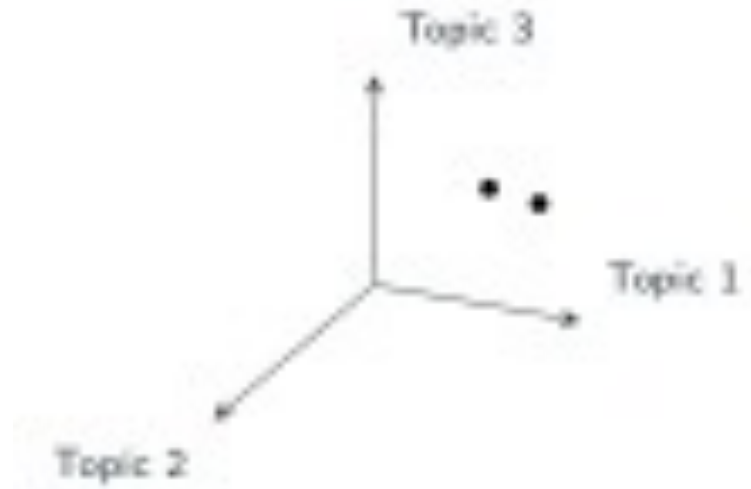
Which behavior makes this observable?

- We model actions that produce cascades on a graph through homophily:

a node imitates a neighbor
if they are similar in ideological
space.

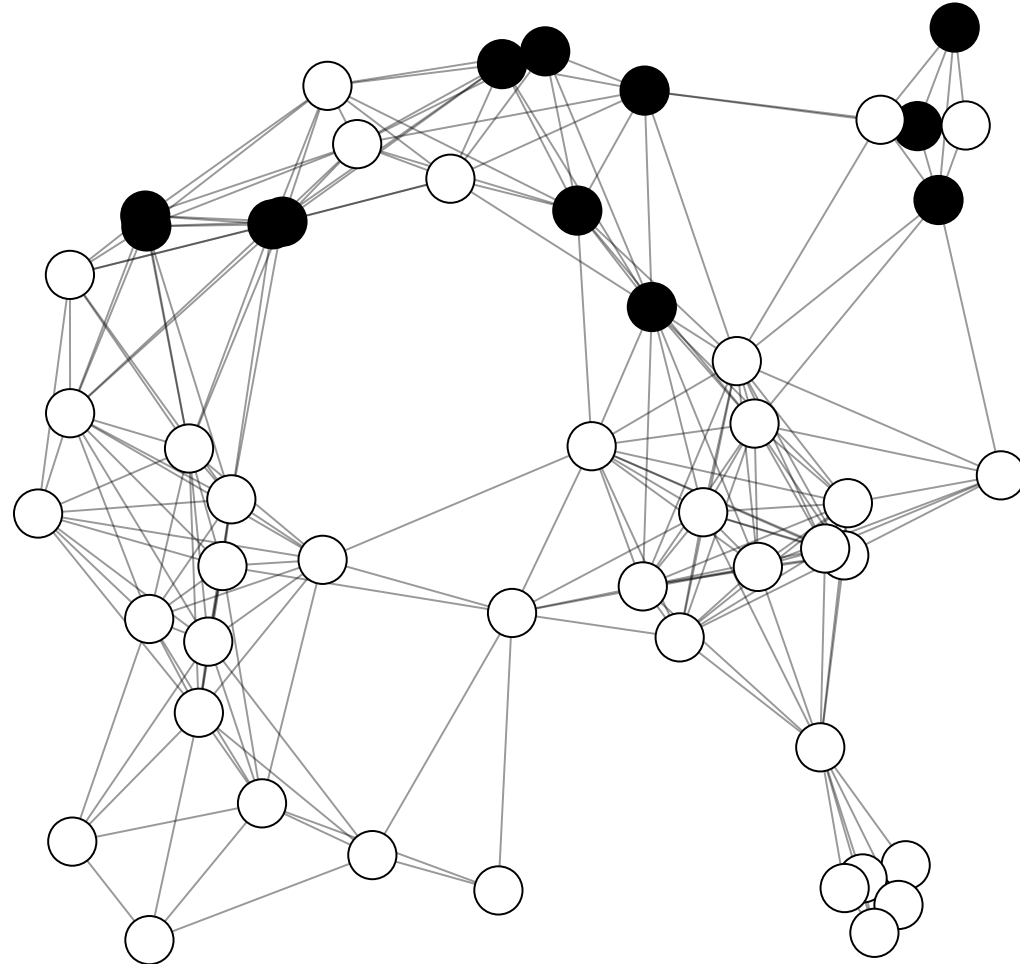
What is an ideological space?

- User-defined
- Each item must be tagged
 - a news can be “healthcare’ or “migration”
 - Manually or LDA
 - Can be fuzzy



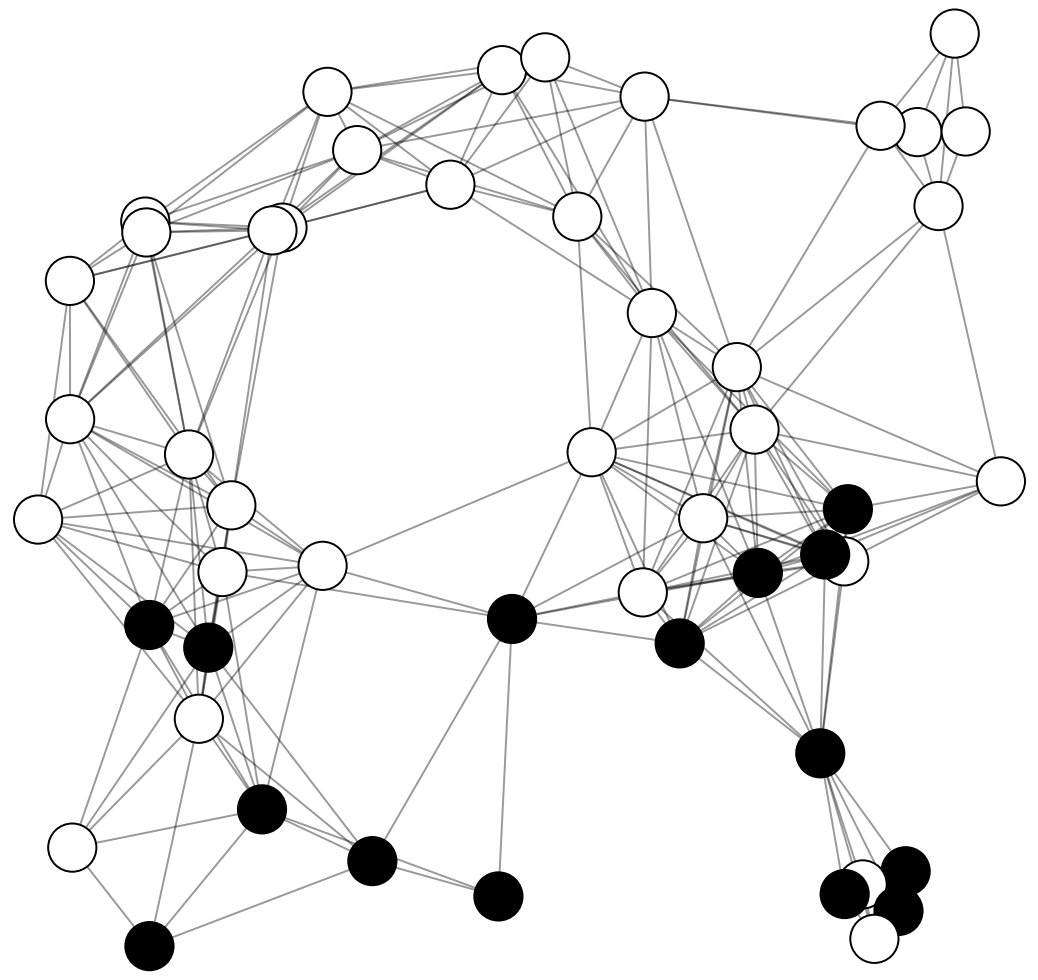
○ = user, ● = user sharing an item

Item 1
0.9 healthcare + 0.1 migration



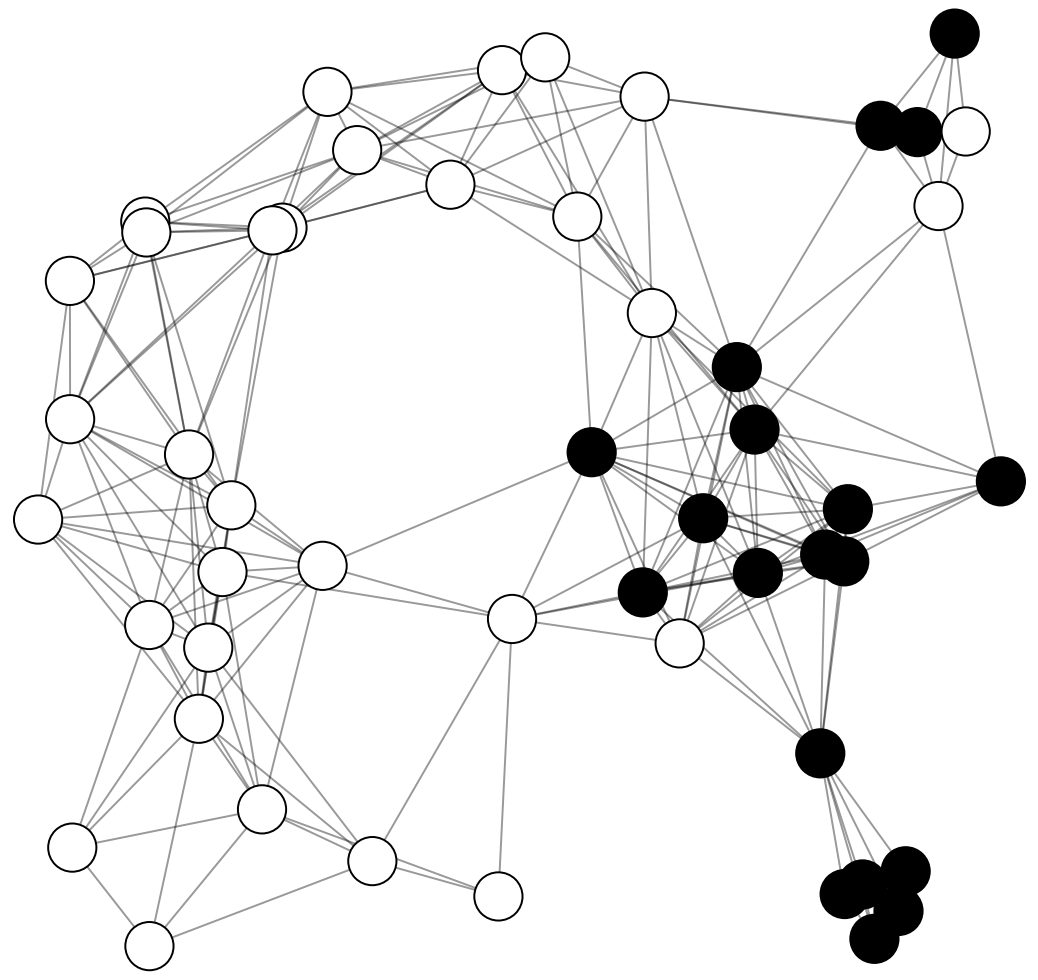
○ = user, ● = user sharing an item

Item 2
0.9 healthcare + 0.1 migration



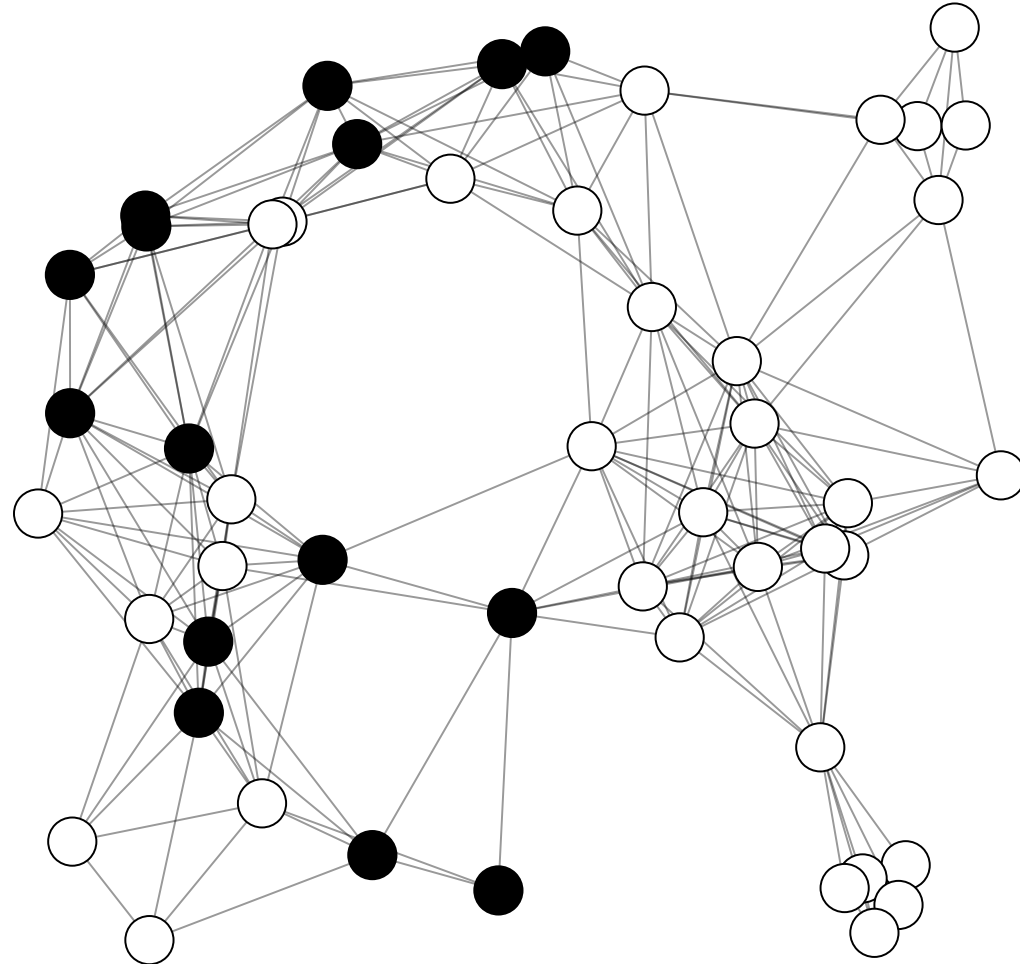
○ = user, ● = user sharing an item

Item 3
0.1 healthcare + 0.9 migration

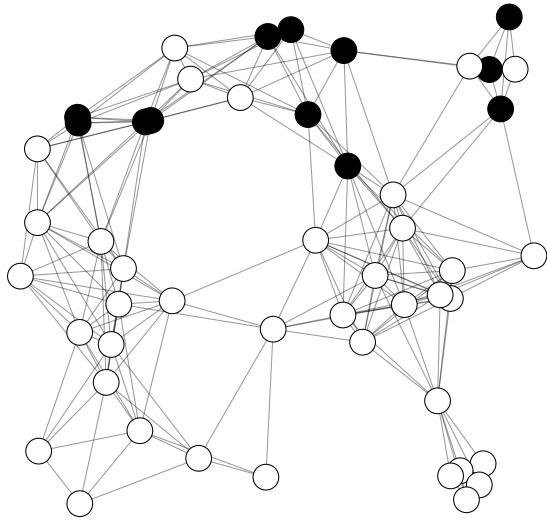


○ = user, ● = user sharing an item

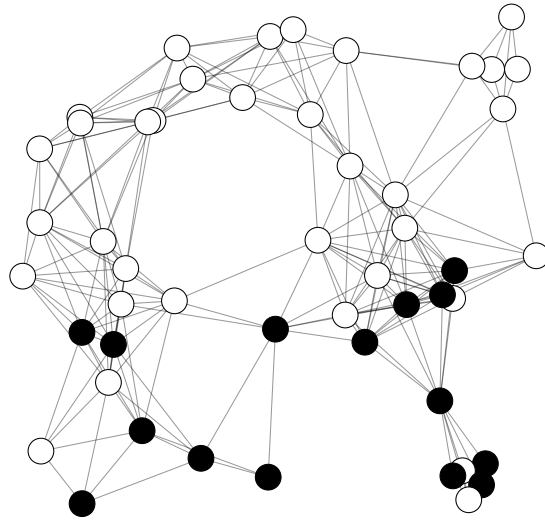
Item 4
0.1 healthcare + 0.9 migration



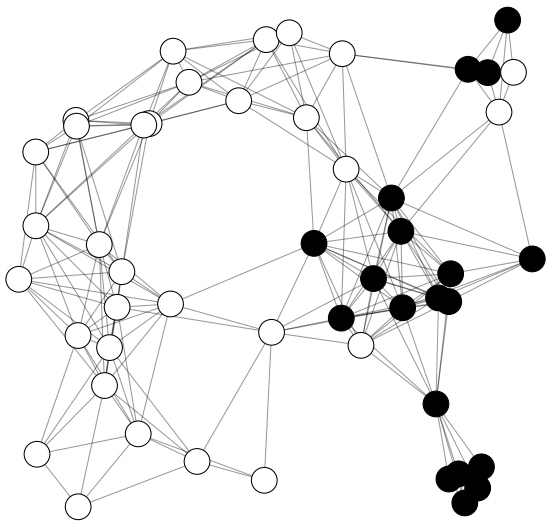
Item 1
0.9 healthcare + 0.1 migration



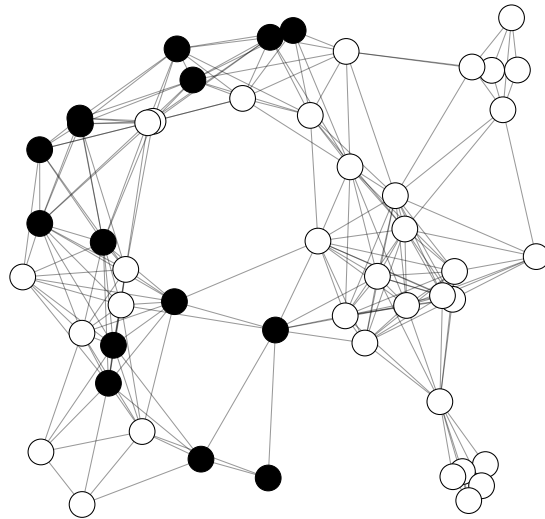
Item 2
0.9 healthcare + 0.1 migration



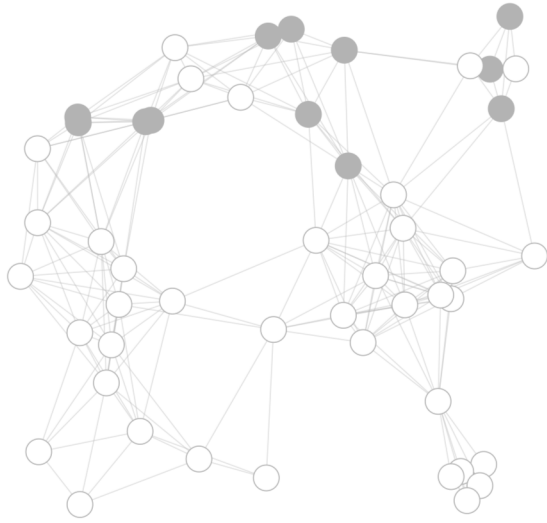
Item 3
0.1 healthcare + 0.9 migration



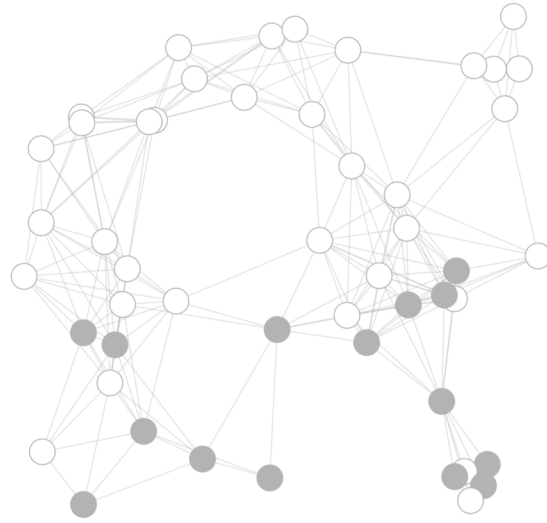
Item 4
0.1 healthcare + 0.9 migration



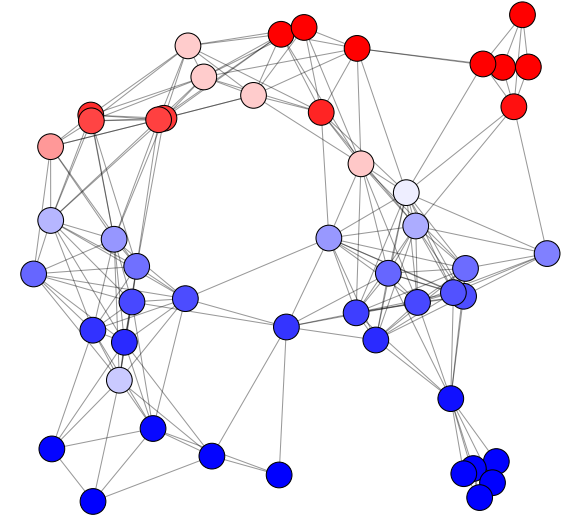
Item 1
0.9 healthcare + 0.1 migration



Item 2
0.9 healthcare + 0.1 migration



Healthcare



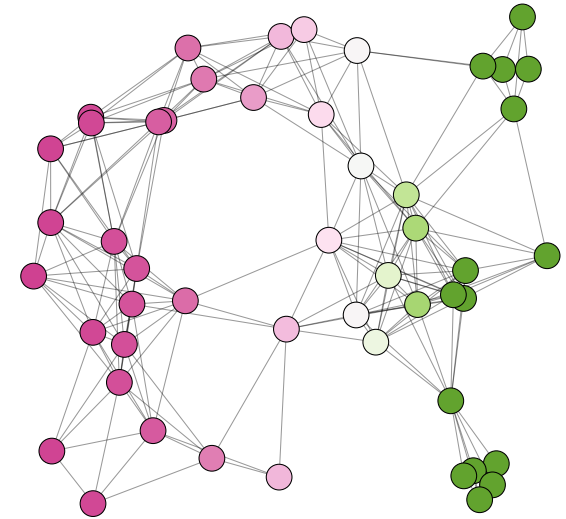
Item 3
0.1 healthcare + 0.9 migration



Item 4
0.1 healthcare + 0.9 migration



Immigration



The Generative model

- Interests $\vartheta_{u,k} \sim \text{Beta}(\alpha, \beta)$
- Polarities $\phi_{u,k} \sim \text{Beta}(p^{-1}, p^{-1})$
- Generate an item i :
 - topic distribution $\gamma_i \sim \text{Dir}(\mathbf{q})$
 - initial activator $v_i \sim U(V)$
 - For $(v, u) \in E$ s.t. v activated and u has not seen i :
 1. Node u sees i from v
 2. topic $k \sim \text{Multinom}(\gamma_i)$
 3. u is interested with probability $\vartheta_{u,k}$
 4. If interested, attitudes of u and v are Bernoullis with $\phi_{u,k}$ and $\phi_{v,k}$
 5. If equal attitudes, u activates on i

Modeling diffusion as ideological alignment

$$\mathcal{L}(i, u) \approx \sum_v \{y_{i,u} \cdot \log(P_{u,v}^{i,+}) + (1 - u_{i,u}) \cdot \log(1 - P_u^{i,+})\}$$

$$P_{u,v}^{i,+} = \sum_k \gamma_{i,k} \cdot \theta_{u,k} \cdot p(u, v, k)$$

Relevance

Interest

Alignment in polarities

Polarity alignment

$$p(u, v, k) = \underbrace{\phi_{u,k} \cdot \phi_{v,k}}_{\text{Positive alignment}} + \underbrace{(1 - \phi_{u,k}) \cdot (1 - \phi_{v,k})}_{\text{Negative alignment}}$$

Learning the model

$$\mathcal{L}(i, u) \approx \sum_v \{y_{i,u} \cdot \log(P_{u,v}^{i,+}) + (1 - u_{i,u}) \cdot \log(1 - P_u^{i,+})\}$$

- Fast and effective gradient-based optimization
 - Each potential activation $u \rightarrow v$ is an example
 - Scales to a large number of cascades
- Extensible to support variational inference

Algorithm 1 Inference algorithm.

Input:

- Graph (V, E)
- For every item $i \in \mathcal{I}$:
 - Its topic distribution γ_i on K topics
 - Its activated nodes $\mathcal{D}_i \subseteq V$

Output: Polarities ϕ_u and interests θ_u for all $u \in V$.

```
1: Initialize  $\phi$  and  $\theta$  as  $|V| \times K$  matrices.
2: for number of epochs do
3:   for  $i \in \mathcal{I}$  do
4:     for  $v \in \mathcal{D}_i$  do
5:       for  $u \in \{u \in \mathcal{D}_i | (v, u) \in E\}$  do
6:         Update  $\phi, \theta$  by ascending the gradient:
          
$$\nabla_{\phi, \theta} \log \left( \sum_k \gamma_{i,k} \cdot \theta_{u,k} \cdot p(u, v, k) \right)$$

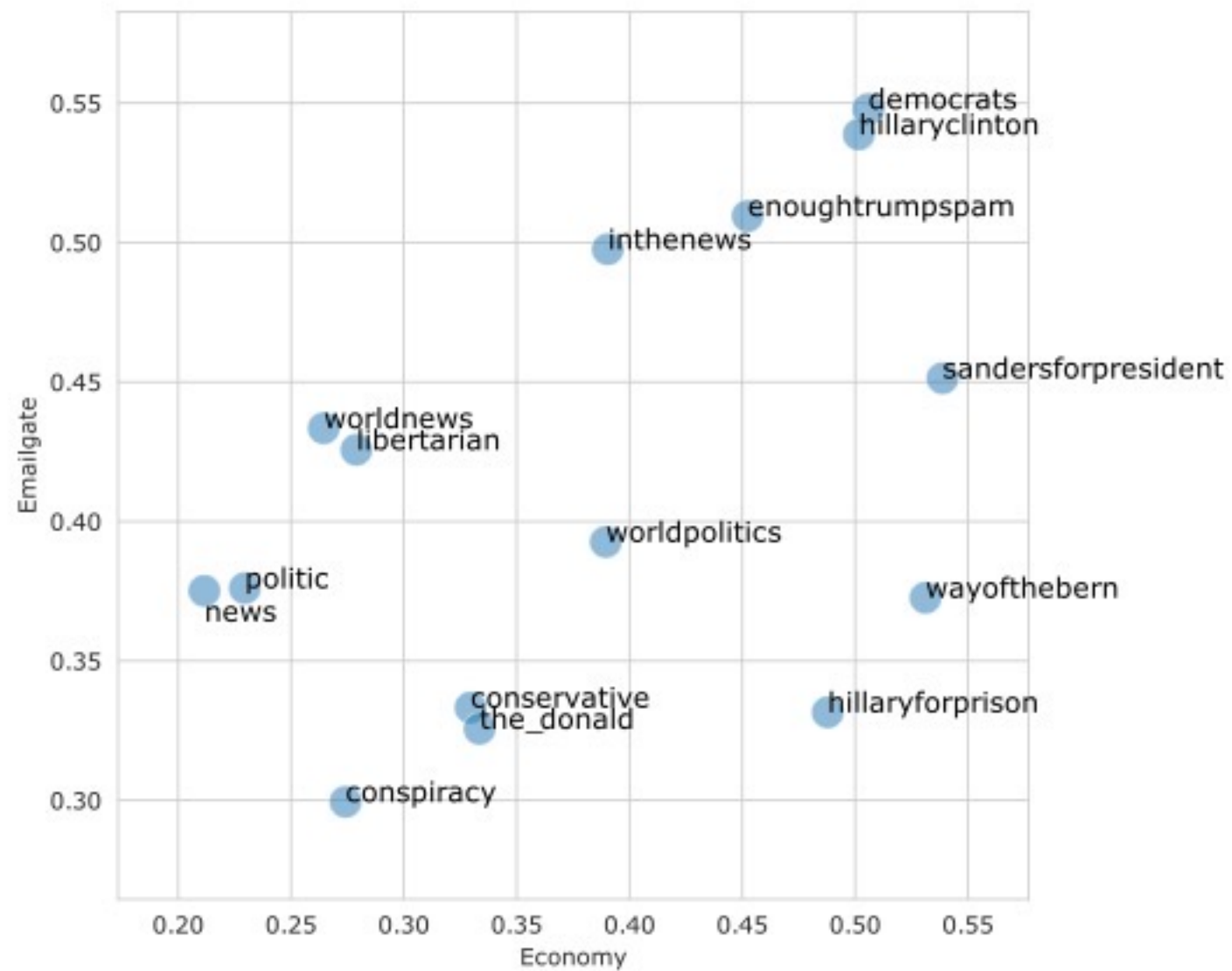
7:       end for
8:       for  $u \in \text{SAMPLE}(\{u \notin \mathcal{D}_i | (v, u) \in E\})$  do
9:         Update  $\phi, \theta$  by ascending the gradient:
          
$$\nabla_{\phi, \theta} \log \left( 1 - \sum_k \gamma_{i,k} \cdot \theta_{u,k} \cdot p(u, v, k) \right)$$

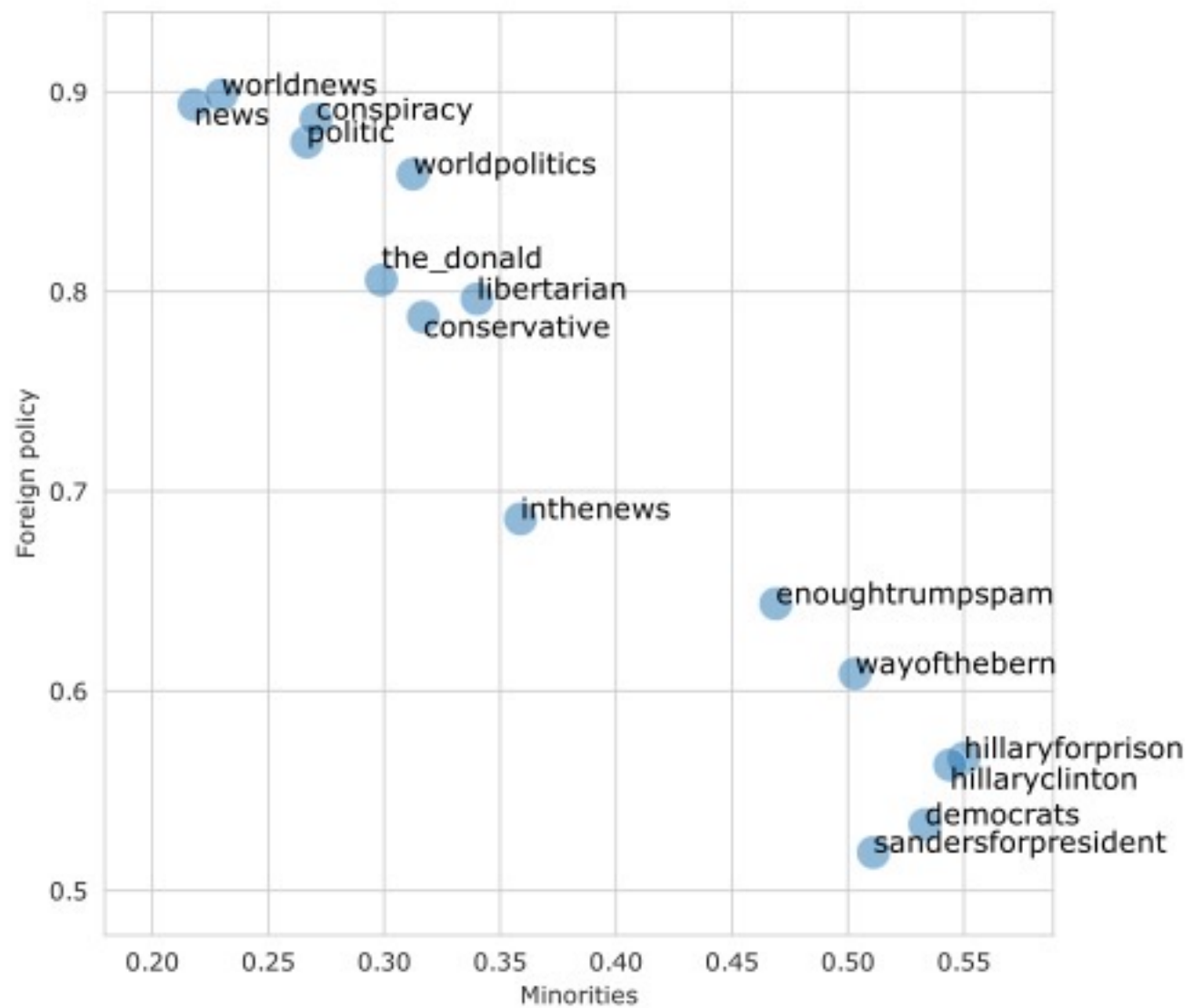
10:      end for
11:     end for
12:   end for
13: end for
14: Return  $\phi$  and  $\theta$ .
```

Results

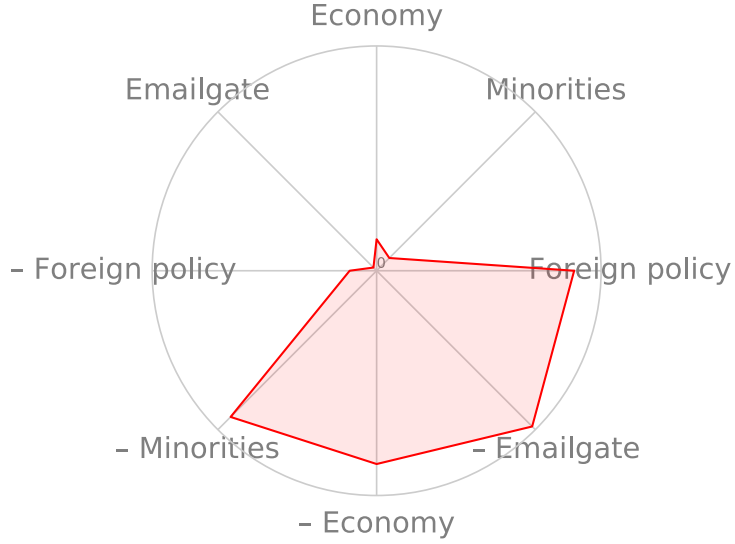
Real data & Interpretability

- Reddit
 - Nodes: 50 political subreddits
 - Actions: Posting a Url
 - 22.047 items
 - 5 topics identified
 - Economy, emailgate, Foreign policy, Campaign, Minorities

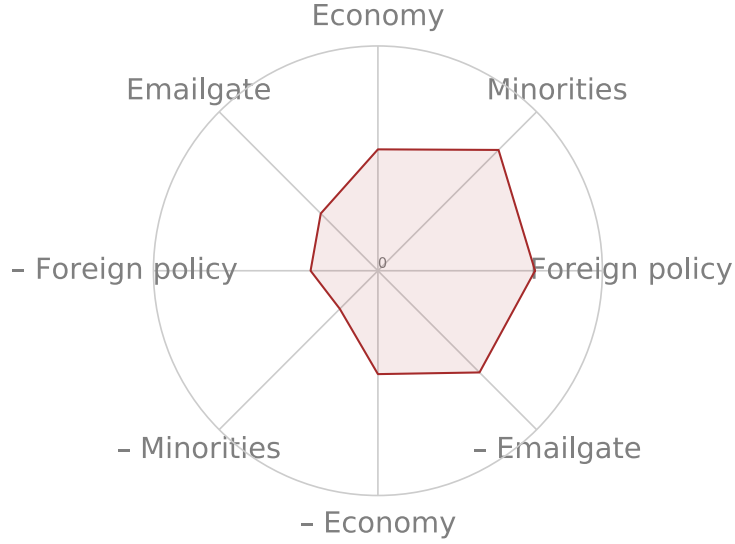




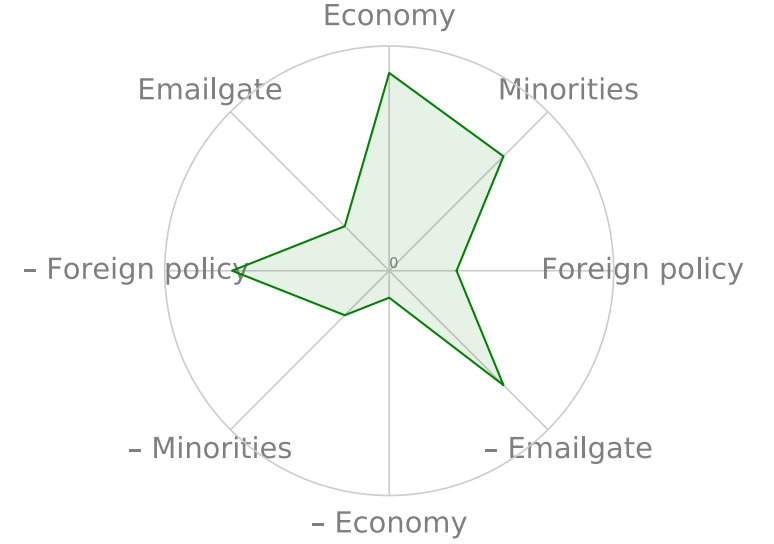
the_donald



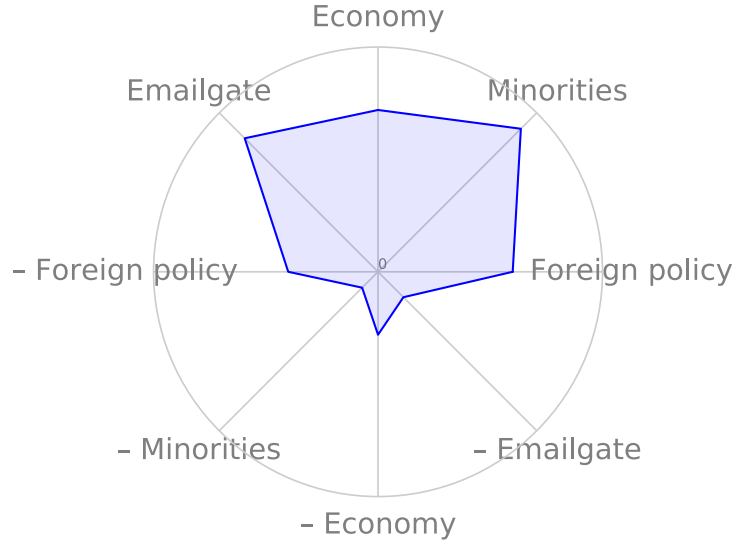
republican



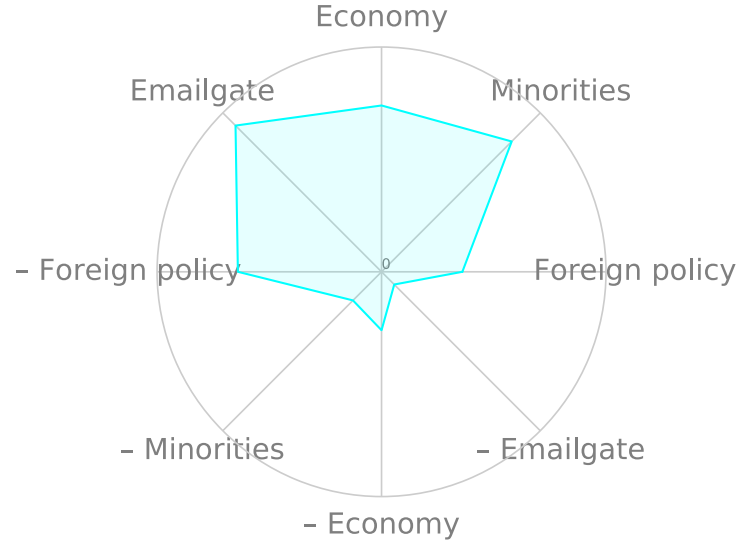
sandersforpresident



hillaryclinton



democrats



Conclusions

- Representation learning for modeling information propagation
 - Susceptibility and influence
 - Interest and relevance
 - Speed of the propagation process
 - Polarity and alignments
- Advantages
 - Interpretability, predictive power, scalable learning
- A unified perspective
 - Can we put all these pieces together?
- Why is it important?
 - Echo-chamber detection
 - Moderating discussions, mitigation policies
 - Fighting misinformation

Thank you

Questions?



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@beman

